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## RESEARCH ARTICLE

# EXPERIMENTAL EVALUATION OF SILL CONFIGURATIONS IN STILLING BASINS FOR EFFICIENT ENERGY DISSIPATION IN HYDRAULIC STRUCTURES

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## ABSTRACT

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Improving energy dissipation and efficiency in hydraulic structures such as spillways, sluices, and weirs, is important to prevent downstream erosion and structural damage under high velocity (supercritical) flows. However, conventional stilling basin designs often fail to optimize hydraulic jump characteristics, particularly under strong hydraulic jump conditions. This study experimentally evaluates the hydraulic performance of single sill and double sill configurations of stilling basin in a laboratory-scale stilling basin under strong hydraulic jump conditions ( $11 < F_1 < 13.2$ ). A series of physical model experiments was conducted by varying sill geometry, height, and spacing. The results showed that the double sill configuration in Series DS-5, combination of an ogee sill ( $Z_1 = 6$  cm) and a trapezoidal prism sill ( $Z_2 = 4.5$  cm) spaced at  $L_1 = 80$  cm,  $L_2 = 0.5L_1$  (40 cm), provides superior hydraulic performance compared to single sill and horizontal apron configurations. Series DS-5 achieved the lowest  $y_2$  and  $y_b$ , the highest relative energy dissipation ( $(E_0 - E_2)/E_0 = 81.42\%$ ), and average energy efficiency ( $E_2/E_1 = 51.31\%$ ). The enhanced performance is attributed to intensified turbulence interaction and improved hydraulic jump control induced by combined sill geometry. Regression based relationships between dimensionless hydraulic variables were also developed to support predictive design. This research contributes a practical and compact stilling basin design for high energy flow conditions, offering improved efficiency and potential application in hydraulic structure design.

## KEYWORDS

Hydraulic jump, Stilling basin, Energy dissipation, Single ogee sill, Double sill, Hydraulic modeling, Froude number

## 1. INTRODUCTION

Hydraulic models are fundamental to the design and optimization of energy dissipation structures, particularly stilling basins, which transition supercritical flows into subcritical flows at downstream of hydraulic structures such as spillways and sluices (Rabiei et al., 2023; Idfi et al., 2024; Al-Mansori et al., 2020; Kumcu and Ispir, 2022; Erryanto and Dermawan, 2024; Chanson, 2022; Al-Fatlawi et al., 2020). Effective stilling basin design is critical to dissipating energy and preventing erosion or structural failure (Raza et al., 2023; Nasiri et al., 2012; Zaffar et al., 2023). A persistent challenge lies in predicting hydraulic jump characteristics and achieving efficient dissipation within limited basin length (Fatimah et al., 2023; Liu et al., 2020; Hadi and Al-Qaisi, 2025; El-Saie et al., 2023). Geometric sill modification has proven effective in enhancing hydraulic performance by stabilizing jumps and influencing turbulence intensity and energy (Jiang et al., 2025; Al-Talib et al., 2019; Al-Fatlawi et al., 2020; Hadi and Al-Qaisi, 2025; Mahmoud and Mohamed, 2022; Zaffar and Hassan, 2023). Variation in sill height, shape, and position markedly affect sequent depth, jump length, and dissipation efficiency (Zhou et al., 2023; Mohammed Saleh and Khassaf, 2023; Tajabadi et al., 2018). The interaction between flow dynamics, sill-induced vortices, and basin geometry complicates the identification of optimal configurations. Recent studies have advanced sill-based design, though remain limited to

simplified geometries, neglecting sustainability and adaptability (Zaffar and Hassan, 2023; Liu et al., 2020; Benabid et al., 2024). Numerical analyses have evaluated performance across configurations, but comprehensive assessment of combined sill types, such as ogee and trapezoidal prism forms, are scarce (Li et al., 2021; Roy et al., 2021; El-Saie et al., 2023; Roushangar and Homayounfar, 2019; Tan et al., 2025; Roy et al., 2021; Dharmadhikari and Gandhi, 2025; Kumar Jayant and Jhamnani, 2024). This gap highlights the potential of double sill systems, which may intensify turbulence, shorten jump, and mitigate scour (Erryanto and Dermawan, 2024; Saleh and Khassaf, 2024). However, the performance under high Froude numbers remains insufficiently validated.

This study introduces novel of single and double sill configurations, hypothesizing improved energy dissipation efficiency and reduced jump length. Laboratory scale experiments evaluate single and double sill configurations, quantifying energy loss and hydraulic jump. In addition, regression-based relationships between hydraulic variables and dimensionless parameters are developed to support predictive design. The findings of this research are expected to provide a practical framework for optimizing stilling basin design, particularly for compact, stable, and efficient energy dissipation systems in high-Froude number hydraulic structures ( $11 < F_1 < 13.2$ ).

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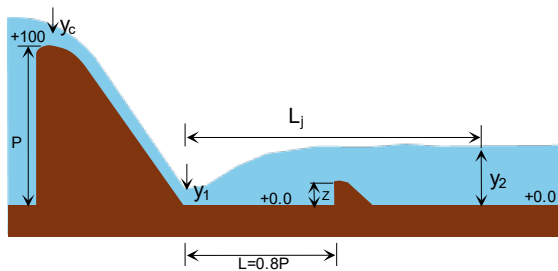
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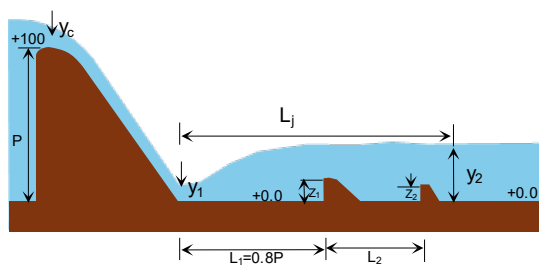
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## 2. MATERIALS AND METHODS

The research was conducted at the River Engineering Laboratory, Universitas Brawijaya. The channel model had a width of 40 cm, wall height of 60 cm, spillway slope of 1:0.8 and height of 100 cm. The measurements carried out were flow depth ( $y_c, y_1, y_2$ ), velocity ( $v_c, v_1, v_2$ ), and the height and length of hydraulic jump ( $y_j, L_j$ ) (Figure 1). The study was conducted using seven (7) flow rates: 15, 17, 19, 21, 23, 25, and 27 liters/second.



(i) Single ogee sill



(ii) double sill (ogee and trapezoidal prism)

**Figure 1:** Hydraulic model in the laboratory and observed hydraulic parameters

Model calibration and verification are performed by comparing the analytical calculation results (expected) with the measurement on the model (observed). Analytical calculations are based on the law of flow continuity, the law of energy conservation, and the conjugation depth.

$$v = \frac{1}{n} R^{2/3} S^{1/2} \tag{1}$$

$$y_c = \sqrt[3]{\frac{Q^2}{B^2 g}} = \sqrt[3]{\frac{q^2}{g}} \tag{2}$$

$$F = \frac{v}{\sqrt{g y}} \tag{3}$$

$$\frac{y_2}{y_1} = \frac{1}{2} \sqrt{1 + 8 F_1^2} - 1 \tag{4}$$

$$E = y + \frac{v^2}{2g} \tag{5}$$

$$MAPE = \frac{100\%}{n} \sum_{i=1}^n \left| \frac{y_i - \hat{y}_i}{y_i} \right| \tag{6}$$

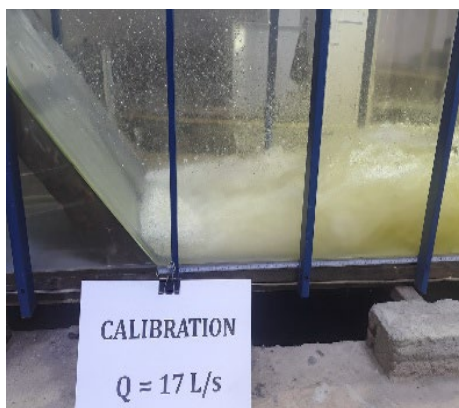
Where:  $y_c$  = critical depth (m),  $Q$  = discharge ( $m^3/s$ ),  $q$  = discharge per unit width ( $m^2/s$ ),  $v$  = velocity (m/s),  $B$  = channel width (m),  $g$  = gravitational acceleration ( $m/s^2$ ),  $E$  = flow energy (m),  $y$  = flow depth (m), MAPE = means absolute percentage error (%).

To strengthen the statistical interpretation of the experimental data, additional graphical analyses were included, such as hydraulic parameters regression plots and dimensionless hydraulic parameters relationships. These diagrams provide visual validation of the statistical correlation ( $R^2$  values) and make the regression predictive model yielded in this study more intuitive. The plots presenting the data allow clearer identification of trends, data dispersion, and the reliability of the proposed equations.

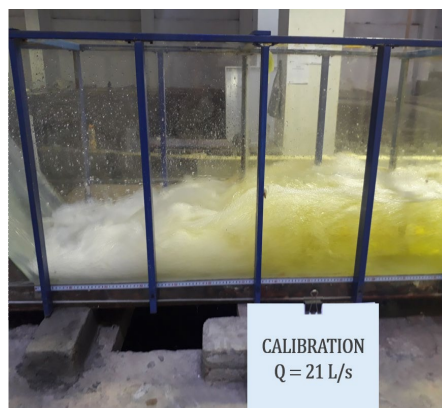
The main hydraulic properties are spillway slope 1:0.8,  $n$  Manning=0.009. Froude number ( $F_1$ ) in this case is  $11 < F_1 < 13.2$  as shown in Table 1. The strong hydraulic jump was formed,  $F_1 > 9$ . By flowing the discharge according to  $y_c$ , the  $y_1$  and  $y_2$  are examined with high accuracy. Figure 2 shows an overview of part of calibration process to investigate  $y_1$  and  $y_2$ .

**Table 1:** Analytical calculation of hydraulic parameters on the model

Q	B	q	$y_c$	$E_0 = E_c$	$v_c$	$y_1$	$v_1$	$F_1$	$y_2$	$v_2$	$F_2$
(L/s)	(m)	( $m^2/s$ )	(m)	(m)	(m/s)	(m)	(m/s)		(m)	(m/s)	
15	0.015	0.4	0.0375	1.079	0.72	0.0094	3.99	13.14	0.1704	0.22	0.17
17	0.017	0.4	0.0425	1.085	0.75	0.0104	4.09	12.79	0.1830	0.23	0.17
19	0.019	0.4	0.0475	1.092	0.78	0.0114	4.17	12.46	0.1948	0.24	0.18
21	0.021	0.4	0.0525	1.098	0.8	0.0125	4.20	11.99	0.206	0.25	0.18
23	0.023	0.4	0.0575	1.104	0.83	0.0135	4.26	11.70	0.2166	0.27	0.18
25	0.025	0.4	0.0625	1.11	0.85	0.0146	4.28	11.31	0.2267	0.28	0.18
27	0.027	0.4	0.0675	1.115	0.87	0.0156	4.33	11.06	0.2364	0.29	0.19



(a) Q=17 L/s

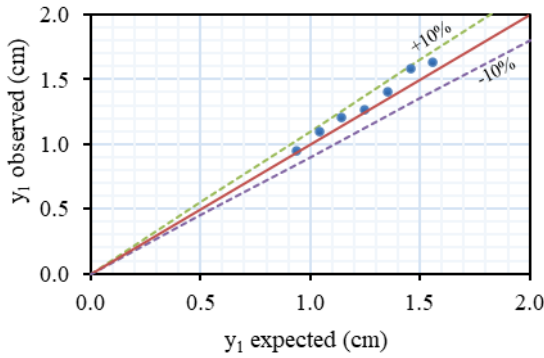


(b) Q=21 L/s

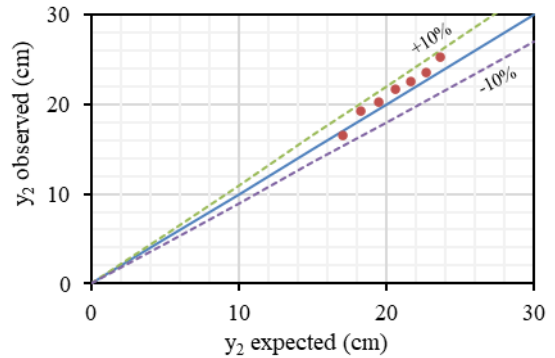


(c) Q=27 L/s

**Figure 2:** Initial hydraulic model running for investigations  $y_1$  and  $y_2$



(a) Scatter plot of  $y_1$  observed vs expected



(b) Scatter plot  $y_2$  observed vs expected

**Figure 3:** Comparison of  $y_1$  and  $y_2$  on model and analytical calculation

Figure 3 represents validation plots between observed and predicted values of  $y_1$  and  $y_2$ , showing strong agreement with low deviation (MAPE<10%). It was found that MAPE  $y_1$  = 4.43%,  $y_2$  = 4.53%,  $F_1$  = 6.20%, and  $F_2$  = 6.46%. The close linear trend confirms the reliability of the model.

**3.1 Single Ogee Sill Stilling Basin**

Observations were made at single ogee sill heights ( $Z$ ) of 10, 8, and 6 cm. The hydraulic jump formed after the single sill is type B. A single ogee sill installed at 80 cm downstream of the spillway toe (Figure 4). Observed data on laboratory of single ogee sill is shown on Table 2.

**3. RESULTS**



(a) Series 1,  $Z=10$  cm,  $Q=21$  L/s



(b) Series 2,  $Z=8$  cm,  $Q=21$  L/s



(c) Series 3,  $Z=6$  cm,  $Q=21$  L/s

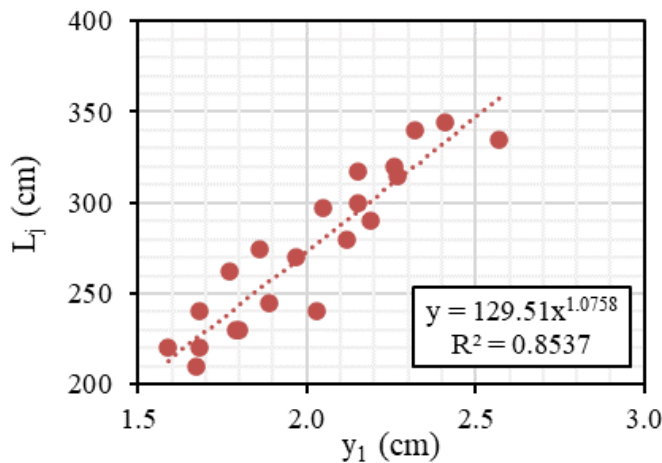
**Figure 4:** Experimental observation of the single ogee sill stilling basin

Table 2: Average values of hydraulic flow parameters in single ogee sill								
Series	Z	L	$y_1$	$y_2$	$y_j$	$L_j$	$(E_0-E_2)/E_0$	$(E_2/E_1)$
	(cm)	(cm)	(cm)	(cm)	(cm)	(cm)	(%)	(%)
SS-1	10	80	2.06	20.40	18.34	272.86	81.14	59.94
SS-2	8	80	2.05	20.86	18.81	273.57	80.73	60.24
SS-3	6	80	1.93	20.30	18.37	279.14	81.22	52.89

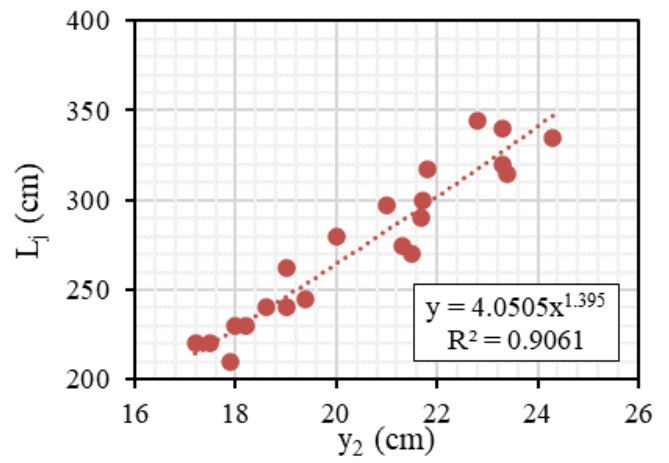
Figure 5 represents regression results of  $L_j$ ,  $y_1$ ,  $y_2$ , and Figure 6 represents the regression among dimensionless parameters for all single ogee sill stilling basin. The variables influencing the jump can be expressed as  $f(y_1, y_2, y_0, v_1, v_2, q, L_j, y_j, Z, g) = 0$ . Following Buckingham's  $\pi$ - theoretical of dimensional analysis and by taking  $y_1$  and  $g$  to be repeated variables, it is possible to derive a dimensionless functional relation based on the

observed data in the laboratory.

Regression lines were fitted to each scatter plot using power law relationships, and the goodness of fit ( $R^2$ ) indicates correlation between hydraulic variables.

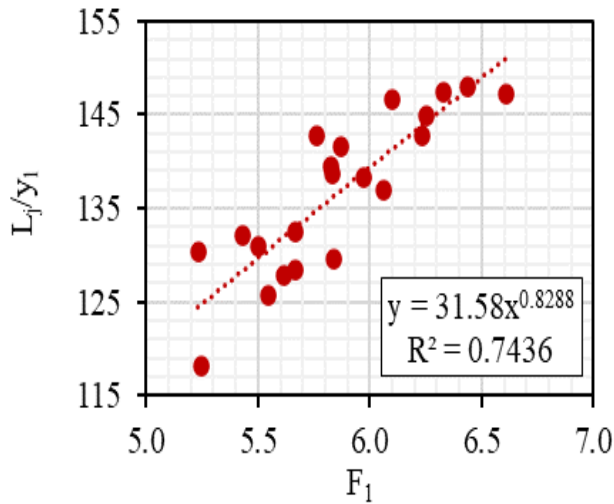


(a) Scatter plot of  $L_j$  vs  $y_1$

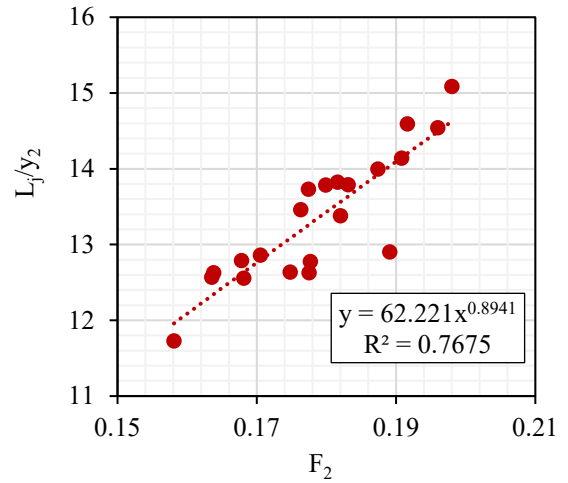


(b) Scatter plot of  $L_j$  vs  $y_2$

**Figure 5:** Relationship between  $L_j$ ,  $y_1$  and  $y_2$  of single ogee sill stilling basin



(a) Scatter plot of  $L_j/y_1$  and  $F_1$



(b) Scatter plot of  $L_j/y_2$  and  $F_2$

**Figure 6:** The relationship between dimensionless parameters on single ogee sill stilling basin

Figure 5 presents that in both cases,  $L_j$  exhibits a strong positive nonlinear relationship, with higher goodness of fit for  $y_2$  ( $R^2=0.9061$ ) compared to  $y_1$  ( $R^2=0.8537$ ), suggesting that  $y_2$  is a more reliable predictor of  $L_j$ . Figure 6 shows both plots exhibit positive power law trends, with moderate to strong correlations. The relationship between  $(L_j/y_2)$  and  $F_2$  ( $R^2=0.7675$ ) shows a slightly better fit than  $(L_j/y_1)$  and  $F_1$  ( $R^2=0.7436$ ), indicating that downstream flow conditions provide a marginally improved prediction of normalized jump length.

To evaluate hydraulic flow performance of sill stilling basin, a scoring method was employed based on ranking, that ranking and score are equal. The optimal series is the lowest cumulative score. The optimal hydraulic

performance is the highest  $y_1$  (decreasing  $F_1$ ), the lowest  $y_2$  and  $y_j$  (reducing height of sidewall), the shortest  $L_j$  (basin requirement), the largest relative energy loss  $(E_0-E_2)/E_0$ , and the smallest ratio of energy before and after hydraulic jump  $(E_2/E_1)$  as shown in Table 3. A lower value of  $(E_2/E_1)$  is considered better because it indicates more effective energy dissipation within the system. It means that a larger portion of the incoming energy has been dissipated. This is desirable in hydraulic engineering, as excess residual energy can lead to downstream issues such as bed erosion, structural damage, and flow instability. Therefore, a smaller  $(E_2/E_1)$  value reflects a more efficient system that better protects downstream areas by minimizing the energy carried by the flow.

**Table 3:** Assessment of hydraulic flow performance in single ogee sill stilling basin

Series	Scores						
	$y_1$	$y_2$	$y_j$	$L_j$	$(E_0-E_2)/E_0$	$(E_2/E_1)$	Cumulative
SS-1	1	2	1	1	2	2	9 <sup>(1)</sup>
SS-2	2	3	3	2	3	3	16 <sup>(3)</sup>
SS-3	3	1	2	3	1	1	11 <sup>(2)</sup>

Note: the number in parentheses indicates ranking

Based on Table 3, the Series SS-1 model provides the optimal results,  $L = 80$  cm,  $Z = 10$  cm, produces the highest  $y_1$ , lowest  $y_j$ , and shortest  $L_j$ .

### 3.2 Double sill stilling basin (ogee and trapezoidal prism)

The double sill is combination of ogee sill ( $Z_1$ ) and a trapezoidal prism sill

( $Z_2$ ). The variation sill distances are  $L_2=0.5L_1$  and  $L_2=0.25L_1$ . The sill height ratio is:  $Z_2=0.75Z_1$  and  $Z_2=0.5Z_1$ . The flow rate was also seven flow rates (Figure 7). Observed data on laboratory of double sill stilling basin is shown on Table 4. The variables influencing the jump were expressed as  $f(y_c, y_1, y_2, v_1, v_2, q, L_1, L_2, Z_1, Z_2, L_j, y_j, g) = 0$ , and the repeated variables were  $y_1$  and  $g$ .



(a) Series DS-1,  $Q = 17$  L/s



(b) Series DS-2,  $Q = 17$  L/s



(c) Series DS-3,  $Q = 17$  L/s



(d) Series DS-4,  $Q = 17$  L/s



(e) Series DS-5,  $Q = 17$  L/s



(f) Series DS-6,  $Q = 17$  L/s

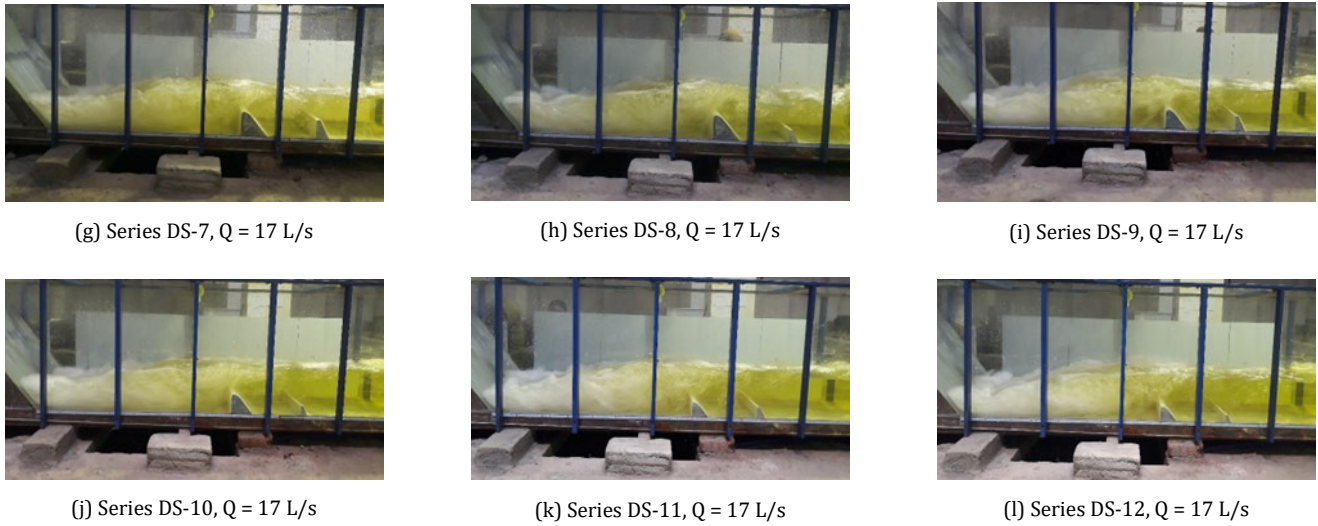


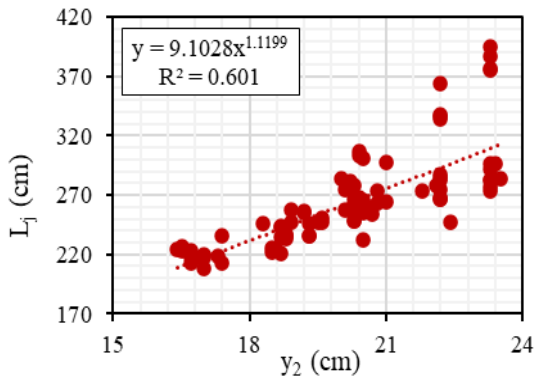
Figure 7: Observation on various configurations of the double sill stilling basin model

Table 4: Average values of hydraulic flow parameters in double sill stilling basin

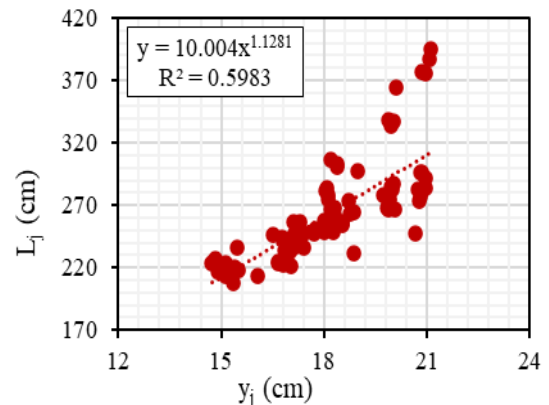
Series	L <sub>1</sub>	L <sub>2</sub>	Z <sub>1</sub>	Z <sub>2</sub>	L <sub>2</sub> /L <sub>1</sub>	Z <sub>2</sub> /Z <sub>1</sub>	y <sub>1</sub>	y <sub>2</sub>	y <sub>j</sub>	L <sub>j</sub>	(E <sub>0</sub> -E <sub>2</sub> )/E <sub>0</sub>	(E <sub>2</sub> /E <sub>1</sub> )
	(cm)	(cm)	(cm)	(cm)			(cm)	(cm)	(cm)		(cm)	(%)
DS-1	80	40	10	7.50	0.50	0.75	2.06	20.01	17.96	264.29	81.47	58.89
DS-2	80	40	10	5.00	0.50	0.50	2.05	20.26	18.21	255.00	81.26	58.65
DS-3	80	40	8	6.00	0.50	0.75	1.93	20.14	18.21	250.00	81.36	52.42
DS-4	80	40	8	4.00	0.50	0.50	2.01	20.26	18.25	257.00	81.26	56.56
DS-5	80	40	6	4.50	0.50	0.75	1.90	20.07	18.17	295.14	81.42	51.31
DS-6	80	40	6	3.00	0.50	0.50	1.91	21.14	19.23	282.29	80.47	53.88
DS-7	80	20	10	7.50	0.25	0.75	2.08	20.14	18.06	245.71	81.36	60.69
DS-8	80	20	10	5.00	0.25	0.50	2.20	20.23	18.03	247.14	81.28	67.36
DS-9	80	20	8	6.00	0.25	0.75	2.12	19.94	17.83	255.86	81.54	61.34
DS-10	80	20	8	4.00	0.25	0.50	2.02	20.09	18.07	256.86	81.41	57.14
DS-11	80	20	6	4.50	0.25	0.75	2.05	20.26	18.21	285.57	81.25	58.24
DS-12	80	20	6	3.00	0.25	0.50	1.99	20.07	18.08	287.57	81.42	56.08

Figure 8 shows the relationship between hydraulic jump length (L<sub>j</sub>) and: (a) y<sub>2</sub>; (b) (y<sub>j</sub>=y<sub>2</sub>-y<sub>1</sub>), on all configurations of double sill stilling basin. L<sub>j</sub> exhibits a positive nonlinear relationship with the independent variables, characterized by similar scaling exponent (~1.12). The coefficients of

determination (R<sup>2</sup>=0.601 for y<sub>2</sub> and R<sup>2</sup>=0.5983 for y<sub>j</sub>) indicate moderate correlation, suggesting comparable predictive capability of y<sub>2</sub> and y<sub>j</sub> for estimating L<sub>j</sub>.



(a) Scatter plot of L<sub>j</sub> vs y<sub>2</sub>



(b) Scatter plot of L<sub>j</sub> vs y<sub>j</sub>

Figure 8: Relationship L<sub>j</sub> with y<sub>2</sub> and y<sub>j</sub> across double sill stilling basin configurations

The power law regression fits in Figure 9 indicates that (y<sub>2</sub>/y<sub>1</sub>) and (y<sub>j</sub>/y<sub>1</sub>) increase with F<sub>1</sub> with similar scaling exponents (~0.72-0.79) and moderate correlation (R<sup>2</sup>≈0.66). (L<sub>j</sub>/y<sub>1</sub>) shows a weaker positive

relationship (R<sup>2</sup>=0.5134), while (E<sub>2</sub>/E<sub>1</sub>) exhibits a strong inverse trend with F<sub>1</sub> (R<sup>2</sup>=0.8682), indicating significant energy dissipation as F<sub>1</sub> increases.

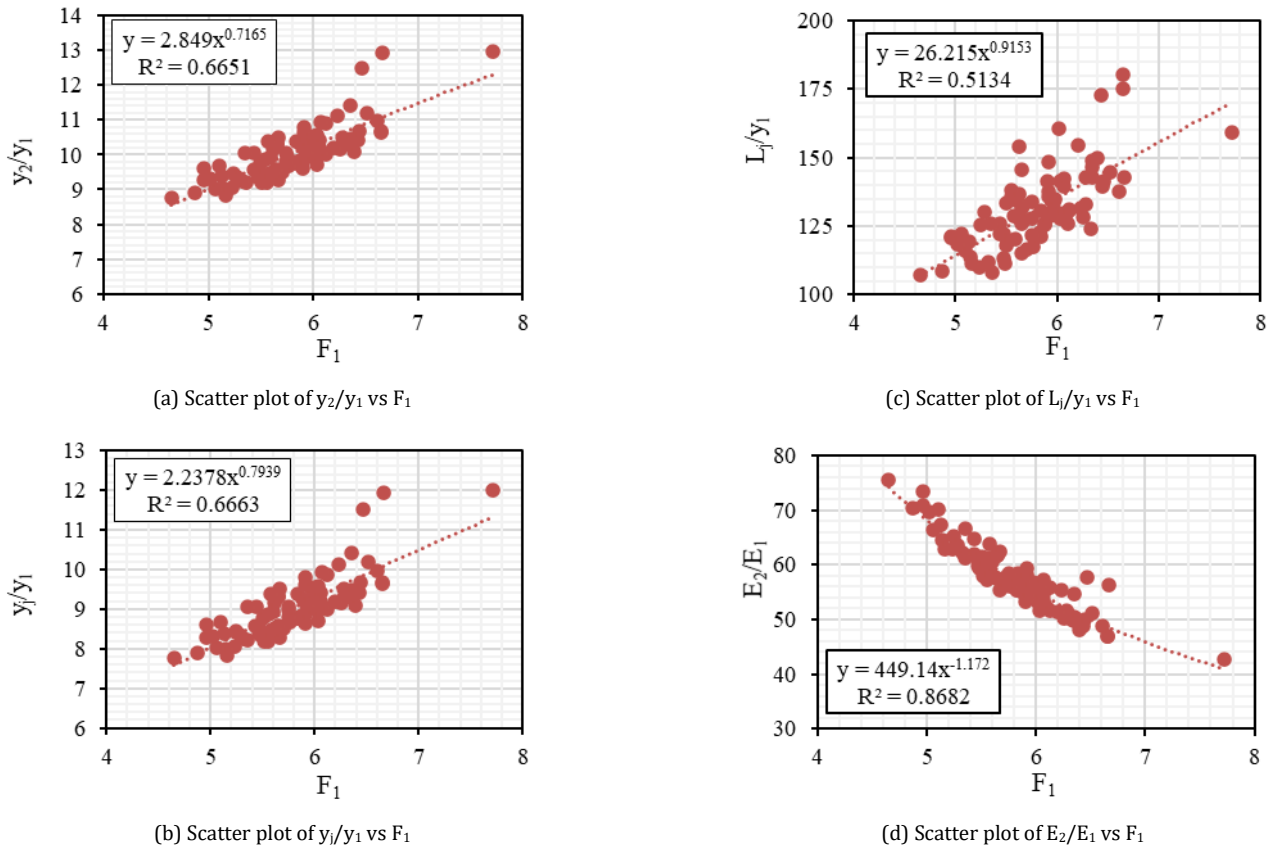


Figure 9: Dimensionless parameters relationship across double sill stilling basin configurations

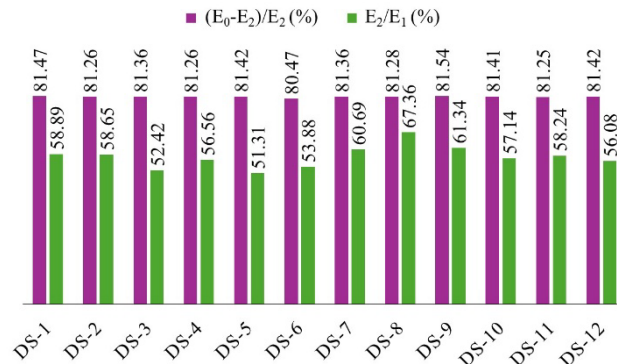


Figure 10: Comparison of energy dissipation characteristics across double sill configurations

The variation in energy dissipation parameters across double sill configurations is shown in Figure 10. The relative energy loss,  $((E_0 - E_2)/E_0)$ , remains fairly consistent, staying within narrow range of about 80-82% for all configurations. This suggests that the total energy dissipation is not significantly affected by changes in the sill configuration. In contrast, the ratio  $(E_2/E_1)$  shows more variation, ranging from 51% to 67%. This indicates that the system depends on the specific configuration. DS-8 exhibits relatively higher  $(E_2/E_1)$  values, meaning less energy is dissipated between sections, whereas DS-5 shows lower values, pointing to more effective localized dissipation. This result suggests that changes in geometry mainly influence how energy is redistributed within the system rather than the total amount of energy dissipated.

The regression analysis shows that hydraulic variables have different levels of correlation. A strong relationship was found for energy efficiency ( $R^2 \approx 0.87$ ), suggesting that this parameter can be predicted with relatively high reliability. In contrast, the jump length relationships and sequent depth relationships showed only moderate correlations ( $R^2 \approx 0.51-0.67$ ), which indicates that other hydraulic processes, such as turbulence interaction and air entrainment, may also influence the observed behavior.

Scoring method on Table 5 is used to obtain the optimal hydraulic flow performance in the double sill stilling basin based on hydraulic flow performance in Table 4. Based on Table 5, Series DS-5 provides the optimal results,  $L_1 = 80$  cm,  $Z_1 = 6$  cm,  $L_2 = (0.5L_1) = 40$  cm,  $Z_2 = (0.75Z_1) = 4.5$  cm, produces the highest  $y_1$  and lowest  $(E_2/E_1)$ .

Table 5: Assessment of hydraulic flow performance in a double sill stilling basin

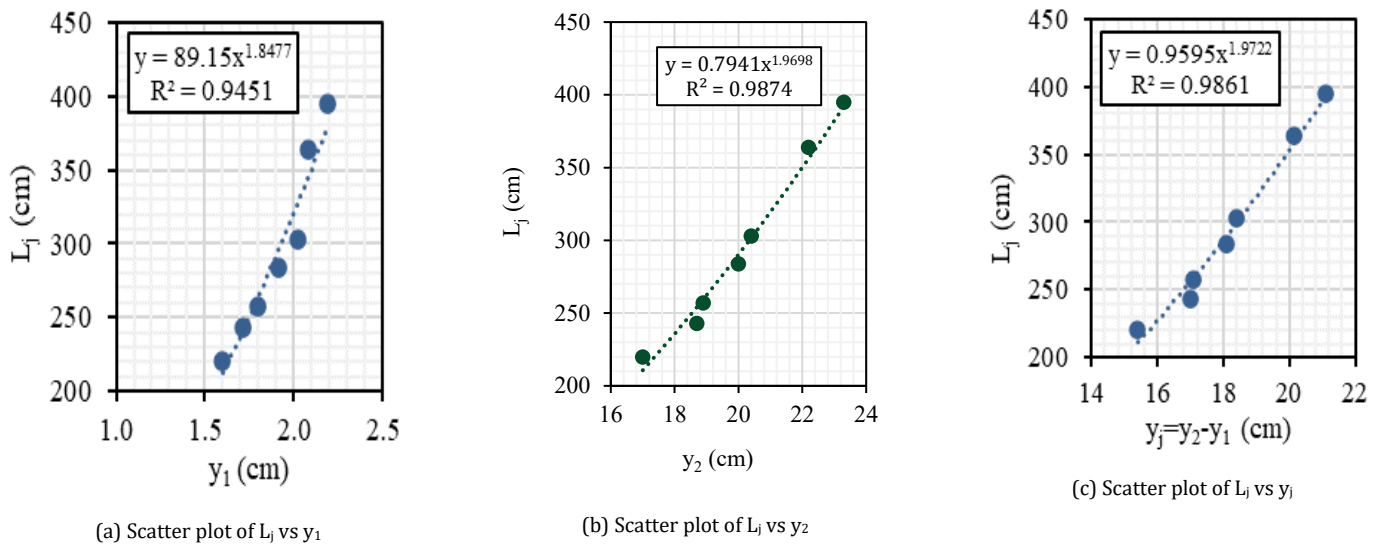
Series	Scores						
	$y_1$	$y_2$	$y_j$	$L_j$	$(E_0 - E_2)/E_0$	$(E_2/E_1)$	Cumulative
DS-1	9	2	2	8	2	9	32 <sup>(4)</sup>
DS-2	7	10	9	4	9	8	47 <sup>(9)</sup>
DS-3	3	6	10	3	7	2	31 <sup>(3)</sup>
DS-4	5	9	11	7	10	5	47 <sup>(10)</sup>

**Table 5:** Assessment of hydraulic flow performance in a double sill stilling basin

Series	Scores						
	y <sub>1</sub>	y <sub>2</sub>	y <sub>j</sub>	L <sub>j</sub>	(E <sub>0</sub> -E <sub>2</sub> )/E <sub>0</sub>	(E <sub>2</sub> /E <sub>1</sub> )	Cumulative
DS-5	1	3	7	12	3	1	27 <sup>(1)</sup>
DS-6	2	12	12	9	12	3	50 <sup>(11)</sup>
DS-7	10	7	4	1	6	10	38 <sup>(7)</sup>
DS-8	12	8	3	2	8	12	45 <sup>(8)</sup>
DS-9	11	1	1	5	1	11	30 <sup>(2)</sup>
DS-10	6	5	5	6	5	6	33 <sup>(5)</sup>
DS-11	8	11	8	10	11	7	55 <sup>(12)</sup>
DS-12	4	4	6	11	4	4	33 <sup>(6)</sup>

Note: The numbers in parentheses indicate ranking.

The regression of hydraulic variables relationship on Series DS-5 such as L<sub>j</sub>, y<sub>1</sub>, y<sub>2</sub>, and y<sub>j</sub> are represented in Figure 11.

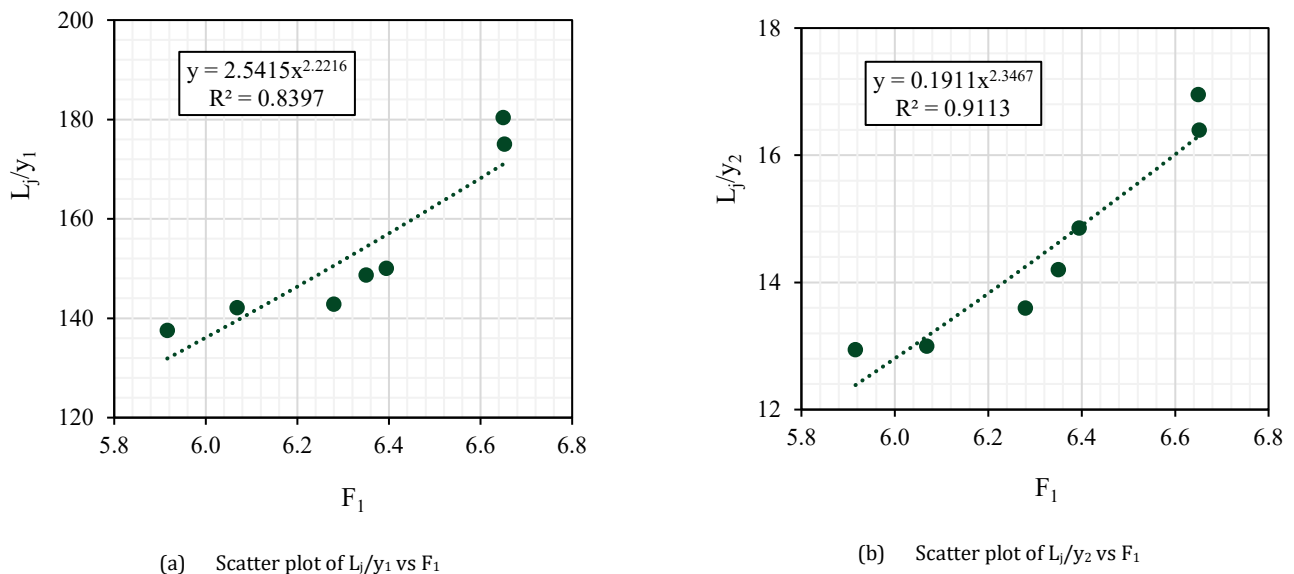


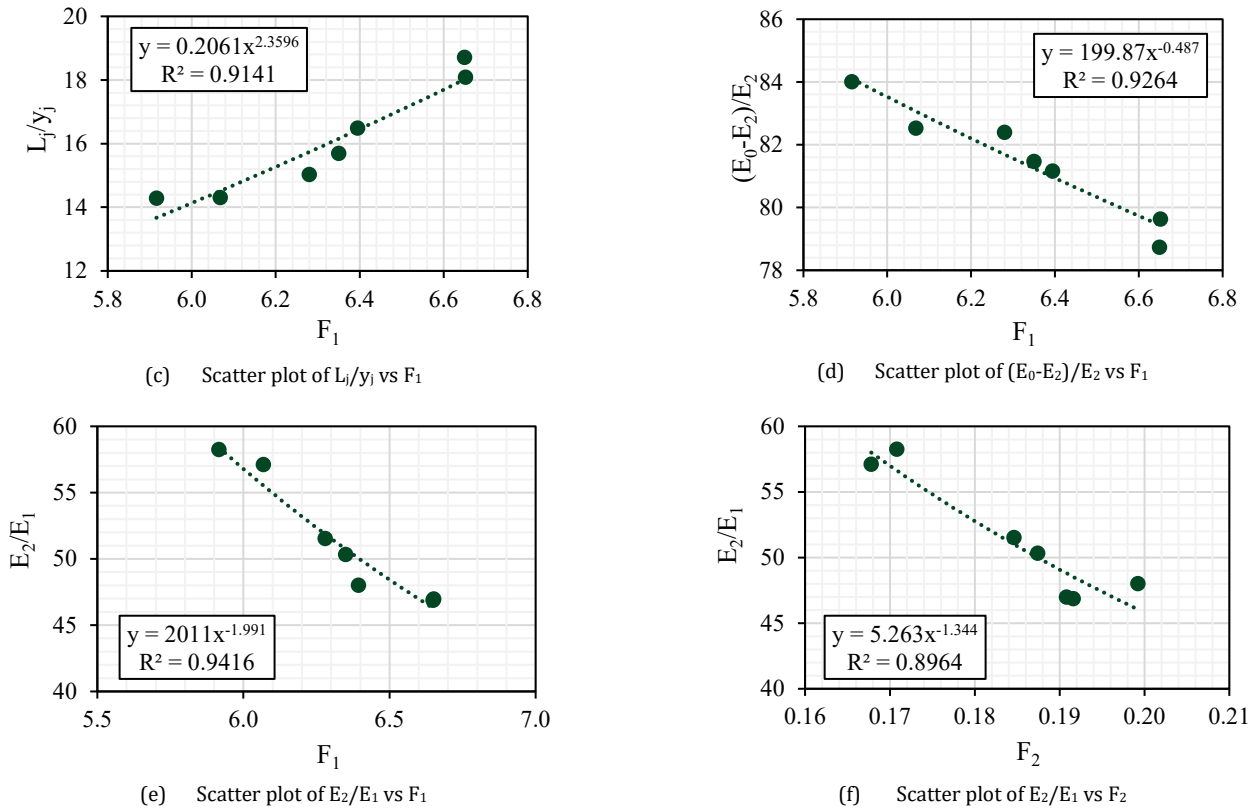
**Figure 11:** Relationships among hydraulic variables in Series DS-5

The statistical relationships in Figure 11 demonstrate that in Series DS-5 the jump length (L<sub>j</sub>) increases consistently with the hydraulic variables y<sub>1</sub>, y<sub>2</sub>, and y<sub>j</sub>. The high R<sup>2</sup> values (≈0.94-0.99), indicate that these variables are strongly associated with the variation in jump length. Among them, y<sub>2</sub> gives the strongest relationship with L<sub>j</sub>, suggesting that the sequent depth is the most reliable predictor of jump length.

The regression among dimensionless parameter relationship on Series DS-5 are represented in Figure 12. The dimensionless parameters relationships in Figure 12 further demonstrate that the hydraulic jump

length parameters (L<sub>j</sub>/y<sub>1</sub>, L<sub>j</sub>/y<sub>2</sub>, L<sub>j</sub>/y<sub>j</sub>) exhibit increasing trends with the Froude number F<sub>1</sub>, indicating that higher incoming flow intensity leads to a longer relative jump length. The corresponding regression equations provide strong fits to the experimental data, with high R<sup>2</sup> values (≈0.83-0.91). Whereas the energy ratios show decreasing trends with increasing Froude number F<sub>1</sub>. This behavior indicates greater energy dissipation at higher flow intensities, confirming the effectiveness of the Series DS-5 configuration in reducing residual flow energy.





**Figure 12:** Relationships among dimensionless parameters in Series DS-5

Table 6 presents the comparison of observed data on hydraulic models of horizontal apron, single ogee sill and double sill stilling basin. The compact stilling basin configuration (ogee and trapezoidal prism, DS-5) exhibits the

highest overall energy dissipation  $((E_0-E_2)/E_0) = 81.42\%$ , while the single ogee sill (SS-1) shows a higher residual energy ratio  $(E_2/E_1) = 59.94\%$ .

Table 6: Comparison of the optimal hydraulic flow parameter on each stilling basin							
Type of Stilling Basin	Series	$y_1$	$y_2$	$y_j$	$L_j$	$(E_0-E_2)/E_0$	$(E_2/E_1)$
		(cm)	(cm)	(cm)	(cm)	(%)	(%)
Horizontal	0	1.31	21.27	19.97	254.29	80.36	25.85
Single Ogee Sill	SS-1	2.06	20.40	18.34	272.86	81.14	59.94
Ogee & Trapezoidal Prism	DS-5	1.90	20.07	18.17	295.14	81.42	51.31

Table 7 presents a comparative scoring analysis of the stilling basin configurations based on key hydraulic parameters within the Froude number range of  $11 < F_1 < 13.2$ . Lower total scores indicate better overall

performance, with the combination of ogee sill and trapezoidal prism sill configuration (DS-5) achieving the best ranking.

Table 7: Best of the optimal series performance scores								
Type of Stilling Basin	Series	$y_1$	$y_2$	$y_j$	$L_j$	$(E_0-E_2)/E_0$	$(E_2/E_1)$	Scores
Horizontal	0	3	3	3	1	3	1	14 <sup>(3)</sup>
Single Ogee Sill	SS-1	1	2	2	2	2	3	12 <sup>(2)</sup>
Ogee & Trapezoidal Prism	DS-5	2	1	1	3	1	2	10 <sup>(1)</sup>

This ranking reflects the improved efficiency of the DS-5 configuration in balancing energy dissipation, flow characteristics, and geometric effectiveness. The results reinforce the advantage of incorporating additional structural elements to optimize hydraulic performance. The statistical diagrams show that the double sill configuration improves hydraulic performance than the single sill configurations. This suggests that the double sill arrangement creates a more stable and predictable flow behavior.

**4. DISCUSSION**

Including statistical diagrams helps make the experimental results easier to interpret. Compared with tables alone, these graphs provide a clearer view of the trends, relationships, and variation within data. The regression plots also show that the proposed empirical equations are reliable and can be applied in engineering design, especially under strong hydraulic jump

condition.

The experimental results clearly demonstrate that double sill configuration significantly enhances the hydraulic performance of stilling basin under strong hydraulic jump conditions. Excellent hydraulic parameters were shown in Series DS-5 with the best parameters in:  $y_2$ ,  $y_j$ , and  $((E_0-E_2)/E_2)$ . The double sill configuration, an ogee sill ( $Z_1 = 6$  cm) and a trapezoidal sill ( $Z_2 = 4.5$  cm) placed at  $0.5L_1$  downstream, offers superior hydraulic performance in energy dissipation, which produced the stable jumps, with kinetic energy conversion into turbulence. The placement of secondary sill downstream of the primary sill plays an important role in controlling the hydraulic jump. The flow experiences a two-stage energy dissipation mechanism: the first sill initiates flow deceleration and partial jump formation, while the second sill enhances turbulence, reinforces roller development, and stabilizes the jump location. This interaction leads to a more controlled and shorter hydraulic jump compared to single sill

stilling basin and horizontal apron stilling basin.

The findings reinforce the analytical framework of (Luo et al., 2021), who located hydraulic jump toe in sloped channels through sequent depth and jump length criteria. The regression-based approach in this study offers a simpler, non-iterate predictive tool of comparable accuracy, enhancing practical applicability. The series DS-5 configuration intensifies turbulence and roller formation, accelerating energy dissipation, and increases downstream depth, thereby mitigating local scour and uplift pressures. This improvement directly addresses failure mechanisms such as those observed in the Liu-Xi River sluice incident (Luo et al., 2021), where neglecting static jump effects compromised structural stability. Across sill-integrated stilling basin, geometry and placement critically influence flow behavior, pressure dynamics, and energy dissipation (Zhou et al., 2023). Bed roughness can reduce basin length by up to 50% while refinements in chute geometry and surface profiling further stabilize hydraulic jumps (Mohammed Saleh and Khassaf, 2023; Saleh and Khassaf, 2024; Fatimah et al., 2023; Macián-Pérez et al., 2020; Liu et al., 2020). Sill-induced turbulence, vortex generation, and air entrainment remain decisive in shaping flow structure and scour risk (Muhamad Bashar et al., 2025; Mahmoud and Mohamed, 2022; Zaffar and Hassan, 2023; Zhao et al., 2020). Double sill systems demonstrate superior performance under high Froude number flows, with calibrated sill height and spacing markedly improving dissipation efficiency and jump stability (Erryanto and Dermawan, 2024; Zhou et al., 2023; Mohammed Saleh and Khassaf, 2023). Numerical analyses confirm their adaptability under variable discharges while roughened beds further enhance turbulence control (Liu et al., 2020; Zaffar and Hassan, 2023). Their effectiveness in energy dissipation and downstream flow stability, indicating the need for continued refinement.

From an engineering standpoint, the enhanced performance of the double sill stilling basin offers significant implications for hydraulic structure design. Its capacity to shorten the hydraulic jump length while sustaining high energy dissipation efficiency enables the development of more compact stilling basins, thereby reducing construction costs and material demands. Moreover, the improvement in jump stability helps mitigate downstream scour and structural damage, ultimately strengthening the safety and long-term resilience of hydraulic systems.

## 5. CONCLUSION

This study aimed to evaluate the hydraulic performance of stilling basins with modified sill configurations. The experimental results demonstrated that the double sill configuration, an ogee sill ( $Z_1 = 6$  cm) and a trapezoidal prism sill ( $Z_2 = 4.5$  cm) spaced at  $0.5L_1$  (40 cm), provided the optimal overall performance. This setup produced the lowest  $y_2 = 20.07$  cm, the lowest  $y_1 = 18.17$  cm, and the highest energy loss  $((E_0 - E_2)/E_0 = 81.42\%)$  along with the average energy dissipation efficiency  $(E_2/E_1 = 51.31\%)$ . Compared to both the horizontal and single sill basins, the Series DS-5 configuration offered superior hydraulic performance. The variation in sill height and spacing significantly influenced flow characteristics, with greater improvements observed in configurations that included a secondary sill placed closer to the primary ogee sill. This arrangement enhanced turbulence generation and stabilized the hydraulic jump effectively.

This study is among the first to experimentally evaluate combined ogee-trapezoidal sill configurations under strong hydraulic jump conditions. This research was conducted at the laboratory scale, under controlled flow conditions, and range of  $11 < F_1 < 13.2$ . The proposed configuration provides a practical design alternative for compact stilling basin design in high-energy hydraulic structures. Potential influences of scale effects, sediment transport processes, and air entrainment dynamics were not explicitly addressed. Consequently, further investigations are necessary to confirm the applicability of the proposed configuration at prototype scale and under more complex hydraulic environments.

Future research should also incorporate numerical modeling and sediment transport analyses to develop a more comprehensive understanding of flow and structure interactions in multi-sill systems.

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